



## Study of electrostatic potential surface and molecular orbitals of O<sub>4</sub> nano cluster by first principles

Onkar Prasad\*, Leena Sinha, Neeraj Misra, Amarendra Kumar, Vijay Narayan, Rajesh Kumar Srivastava, Hriday Narayan Mishra

Physics Department, University of Lucknow, Lucknow, India

---

### Abstract

Study of properties of nanoclusters are important from various fundamental and applications point of view. The study of frontier orbitals, molecular electrostatic potential surface of O<sub>4</sub> oxygen nano cluster in the puckered square (O<sub>4A</sub>) and the pinwheel (O<sub>4B</sub>) geometry has been carried out using the first principles. The MEP surface has been used to predict the active sites for electrophilic and nucleophilic interactions in both the O<sub>4</sub> cluster geometries.

**Key Words:** Frontier orbitals, Nano cluster, MEP, Cluster energy.

---

### Introduction

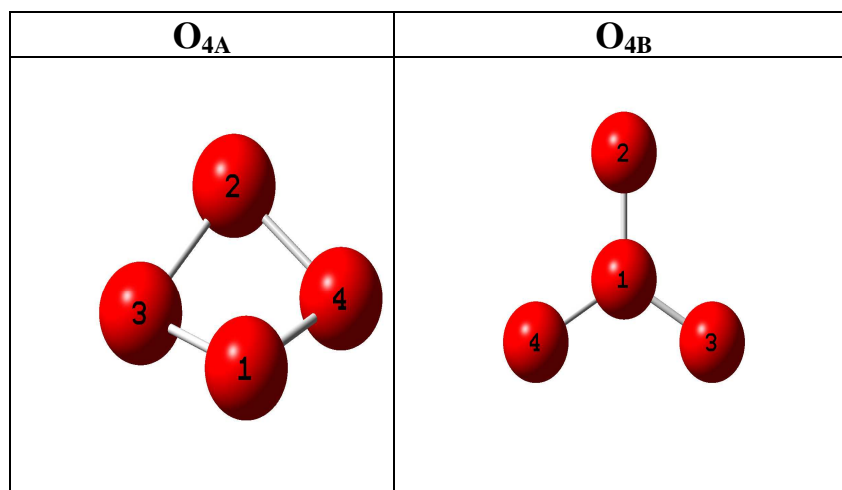
A molecular cluster of oxygen, the tetraoxygen cluster O<sub>4</sub>, known as “oxozone” was predicted in 1924 by Gilbert N. Lewis as an explanation for magnetism of oxygen O<sub>2</sub> molecule, nevertheless metastable O<sub>4</sub> cluster has been recently observed in mass spectroscopy experiments [1]. Devina and others have proposed an adsorption model for molecular oxygen on reduced TiO<sub>2</sub>(110) and have studied the formation of tetraoxygen (O<sub>4</sub>) [2]. Since its discovery, O<sub>4</sub> cluster has been a subject of interest from both experimental as well as theoretical point of view [3-6], because of its potential, being more powerful oxidizer than O<sub>2</sub> or O<sub>3</sub> and therefore may also be used as rocket fuel in future [1].

In the present communication a complete systematic study of structural, energetic properties of O<sub>4</sub> cluster has been carried out using the first principles. With the optimized geometry, the frontier orbitals, electron density and molecular electrostatic potential surfaces of the cluster have been generated with further analysis leading to prediction of stability and activity of the cluster.

## Results and Discussion

The tetraoxygen was proposed as an explanation for the failure of liquid oxygen to obey curie law [13]. Computer simulations have indicated that O<sub>2</sub> molecules associate in pair and form O<sub>4</sub> cluster [14]. The two different geometries: a puckered square (O<sub>4A</sub>) and a pinwheel (O<sub>4B</sub>) in case O<sub>4</sub> [15,16] have been the starting point for the present calculations. The equilibrium geometry optimization of the nano cluster in ground state has been achieved by energy minimization, using DFT/ B3LYP functional with 6-31++G(d,p), cc PVQZ and AUG cc PVQZ basis sets. The optimized molecular structures thus obtained together with the numbering scheme of the atoms is shown in the Fig. 1. and the optimized parameters are given in table 1. The ground state energy of the optimized structure of O<sub>4A</sub> and O<sub>4B</sub> at different basis sets are given in table 2.

**Figure 1: Optimized Geometries of Tetra - Oxygen Cluster**



**Table 1: Optimized Bond Lengths, Angles and Dihedrals of O<sub>4</sub> Cluster**

O <sub>4A</sub>		O <sub>4B</sub>	
R(1,3)	1.5305	R(1,2)	1.2905
R(1,4)	1.5305	R(1,3)	1.2905
R(2,3)	1.5305	R(1,4)	1.2905
R(2,4)	1.5305	A(2,1,3)	120.0
A(3,1,4)	86.7742	A(2,1,4)	120.0
A(3,2,4)	86.7743	A(3,1,4)	120.0
A(1,3,2)	86.7743	L(2,1,3,4,-2)	180.0
A(1,4,2)	86.7743		
D(4,1,3,2)	-26.6893		
D(3,1,4,2)	26.6893		
D(4,2,3,1)	26.6893		
D(3,2,4,1)	-26.6893		

Note: Bond lengths are in Å, angles and dihedrals are in degrees.

**Table 2 : Optimized ground state energies of O<sub>4A</sub> and O<sub>4B</sub> cluster in Hartree**

Functional/Basis Set	O <sub>4A</sub>	O <sub>4B</sub>
B3LYP/ 6-31++G(d,p)	-300.4893	-300.4737
B3LYP/ cc- PVQZ	-300.6220	-300.6078
B3LYP/ aug-cc-PVQZ	-300.6243	-300.6103

According to second derivative analysis, the calculated vibrational spectra for the cluster has no imaginary frequency, therefore the optimized geometry is confirmed to be located at the local minima on potential energy surface (table 3). The intramolecular bond lengths in the O<sub>4A</sub> and O<sub>4B</sub> are calculated to be 1.5305 Å<sup>0</sup> and 1.2905 Å<sup>0</sup>. It is interesting to note that the calculated intramolecular bond length is found to be larger in case of puckered square O<sub>4A</sub> structure and shows the single bond character, whereas the corresponding bond length in case of pinwheel structured O<sub>4B</sub> cluster reflects a partial double bond character, as its value is closer to the standard O=O bond length (1.210 Å<sup>0</sup>). It has been observed theoretically that the ground state energy of the tetra-oxygen cluster decreases with an increase in dimensionality of the basis set. The binding energy and the bond energy of oxygen cluster are reported in the table 4 at the Aug-cc-PVQZ basis sets. Although the ground state energy of O<sub>4A</sub> and O<sub>4B</sub> are almost same but the pinwheel shaped O<sub>4B</sub> cluster seems to be thermally more stable than puckered squared shaped O<sub>4A</sub> cluster, as the calculated bond energy is smaller in later. It is also interesting to note the order of the calculated bond energy for O<sub>4</sub> cluster is Eb O<sub>4B</sub> > Eb O<sub>4A</sub> (refer to Table 4).

**Table 3 : Harmonic Frequencies of O<sub>4A</sub> and O<sub>4B</sub> cluster in cm<sup>-1</sup>**

S.No.	O <sub>4A</sub>	S.No.	O <sub>4B</sub>
1.	397	1.	601
2.	804	2.	601
3.	804	3.	668
4.	861	4.	894
5.	923	5.	1060
6.	1000	6.	1060

**Table 4 : Cluster Energy, Binding Energy and Bond Energy of O<sub>4A</sub> and O<sub>4B</sub> at B3LYP/ AUG-cc-PVQZ**

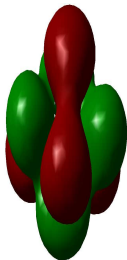
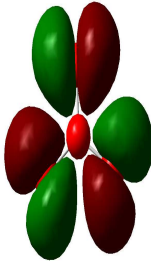
S.N o.	Parameter	O <sub>4A</sub>	O <sub>4B</sub>
1.	Cluster Energy(eV)	-17.2058	-16.82481
2.	Binding Energy (eV/ atom)	-4.3014	-5.6082
3.	Bond Energy (Kcal/mol)	99.1935	129.3297

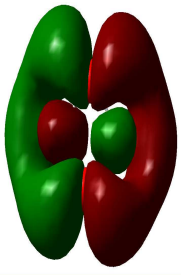
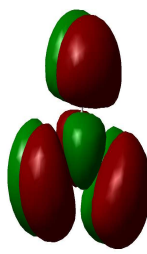


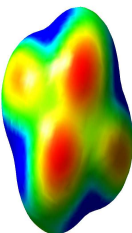
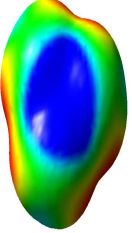
## Electronic properties

The basic electronic parameters related to the frontier orbitals in a molecule are the highest occupied molecular orbital (HOMO) and lowest unoccupied molecular orbital (LUMO) and their resulting energy gap. These orbitals not only determine the way the molecule interacts with other species, but their energy gap (frontier orbital gap) help in characterizing the chemical reactivity and kinetic stability of the molecule. The 3D plots of the HOMO, LUMO, Total Electron Density (TED) and electrostatic potential surface mapped on isodensity surface (MEP) for both the structure of O<sub>4</sub> cluster are shown in fig. 2. The calculated value of frontier orbital energy gap of O<sub>4</sub> having 0.1764 Hartree and 0.1322 Hartree for puckered square and pinwheel shaped structures respectively, is calculated at the same level of theory and the same basis sets. The high frontier orbital gap is associated with a low chemical reactivity and high kinetic stability [17].

The electrostatic potential is a physical property of a molecule related to how a molecule is first “seen” or “felt” by another approaching species. A portion of a molecule that has a negative electrostatic potential is susceptible to electrophilic attack – the more negative the better. The molecular electro-static potential (MEP) map as shown in fig.2., is an important parameter which is related to the electronegativity and the partial charges on the different atoms of the molecule along with the TED. Its study leads to the better

**Figure 2 : Frontier Orbitals, Total Electron Density and MEP of Tetra - Oxygen Cluster**

CLUSTER SURFACES	O <sub>4A</sub>	O <sub>4B</sub>
HOMO		

<b>LUMO</b>		
<b>TOTAL ELECTRON DENSITY</b>		
<b>MEP</b>		

understanding of complex processes involving the charge-dipole, dipole-dipole, and quadrupole-dipole interactions. The red and blue regions in the MEP map refers to the regions of negative and positive potential and correspond to the electron-rich and electron-poor regions respectively whereas the green colour signifies the neutral electrostatic potential. The MEP surface provides necessary information about the reactive sites. The MEP of  $O_4$  reveals some interesting features that in case of puckered square  $O_{4A}$  cluster there are four centres (represented by blue colour) for nucleophilic attack, whereas in spinwheel case there are only two centres for nucleophilic attack, one above and the other below the plane of the tetra-oxygen cluster in  $O_{4B}$  geometry.

## Materials and methods

The *ab initio* calculations reported here, have been carried out using the Gaussian 03, suite of program [7-12] employing density functional theory to investigate the oxygen nano cluster  $O_4$ . The reported geometry, molecular properties such as equilibrium energy, HOMO-LUMO band

gap, dipole moment have also been used to understand the O<sub>4</sub> cluster under investigation. After the geometry optimization, the vibrational frequencies were also calculated. The stability of cluster has been discussed in terms of the total interaction energy V<sub>cluster</sub>, the binding energy B.E. and the bond energy E<sub>b</sub> defined as following:

$$V_{\text{cluster}} = [E_n - nE_1], \text{ B.E.} = V_{\text{cluster}}/n \text{ and } E_b = V_{\text{cluster}}/m$$

Where n is the number of Oxygen atoms and m is the number of O-O bonds in the cluster, E<sub>n</sub> is the cluster energy of O<sub>n</sub> and E<sub>1</sub> refers to the atomic ground state energy.

## Conclusion

The equilibrium geometries of the oxygen cluster O<sub>4</sub> were determined and analyzed at DFT level using B3LYP functional employing 6-31++G(d,p) and cc-PVQZ and AUG-cc-PVQZ basis sets. The harmonic frequencies were determined at AUG-cc-PVQZ basis set. The binding energy, bond energy and frontier orbital energy gap data suggest that the spinwheel structure is kinetically more stable than other puckered squared O<sub>4</sub> cluster under study. The MEP has been used to understand the characteristics of oxygen cluster O<sub>4</sub>. The present quantum chemical study predicts reasonably well the geometric parameters as well as electronic properties and might play an important role in better understanding of the tetra-oxygen cluster.

## Acknowledgement

The authors are grateful to University Grants Commission (UGC), Government of India for providing the financial assistance.

## References

- [1] Fulvio Cacace,; P.D. Giulia, and Troiani Anna; *Angewandte Chemie Int. Ed.* **2001**, 40 (21), 4062–65.
- [2] Devina Pillay, Yun Wang, Gyeong S Hwang; *J Am Chem Soc.*, **2006**, 1,128(43):14000-1.
- [3] I.N. Goncharenko, O.L. Makarova and L. Ulivi. *Phys. Rev.Lett.* **2004**, 93:055502.
- [4] B. Militzer and R. J. Hemley, *Nature* , **2006**, 443, 150.
- [5] S. Desgreniers, Y. K. Vohra, and A. L. Ruoff, *J. Phys. Chem.*, **1990**, 94,1117.
- [6] Yue Meng, Peter J. Eng, John S. Tse, Dawn M. Shaw, Michael Y. Hu, JinfuShu, Stephen A. Gramsch, Chichang Kao, Russell J. Hemley, and Ho- kwang Mao, " Proc. Nat. Acad. Sci. USA 2008, 105(33), 11640.
- [7] M.J. Frisch, G.W. Trucks, H.B. Schlegel, G.E. Scuseria, M.A. Robb, J.R. Cheeseman, J.A. Montgomery Jr., T. Vreven, K.N. Kudin, J.C. Burant, J.M. Millam,S.S. Iyengar, J. Tomasi, V. Barone, B. Mennucci, M. Cossi, G. Scalmani, N. Rega,G.A. Petersson, H. Nakatsuji, M. Hada, M. Ehara, K. Toyota, R. Fukuda, J.Hasegawa, M. Ishida, T. Nakajima, Y. Honda, O. Kitao, H. Nakai, M. Klene, X. Li,J.E. Knox, H.P. Hratchian, J.B. Cross, C. Adamo, J. Jaramillo, R. Gomperts, R.E.Stratmann, O. Yazyev, A.J. Austin, R. Cammi, C. Pomelli, J.W. Ochterski, P.Y.Ayala, K. Morokuma, G.A. Voth, P. Salvador, J.J. Dannenberg,

- V.G.Zakrzewski, S. Dapprich, A.D. Daniels, M.C. Strain, O. Farkas, D.K. Malick, A.D.Rabuck, K. aghavachari, J.B. Foresman, J.V. Ortiz, Q. Cui, A.G. Baboul, S.Clifford, J. Cioslowski, B.B. Stefanov, G. Liu, A. Liashenko, P. Piskorz, I. Komaromi,R.L. Martin, D.J. Fox, T. Keith, M.A. Al-Laham, C.Y. Peng, A. Nanayakkara, M.Challacombe, P.M.W. Gill, B. Johnson, W. Chen, M.W. Wong, C. Gonzalez, J.APople, Gaussian 03, Gaussian, Inc., Pittsburgh, PA, **2003**.
- [8] R.Dennington, T. Keith, J. Millam, K. Eppinnett, W.L. Hovell, R. Gilliland, GaussView, Version 3.07, Semichem, Inc., Shawnee Mission, KS, **2003**.
- [9] W. Kohn, L.J. Sham , *Phys. Rev.*, **1965**, 140 A1133-A1138.
- [10] A.D. Becke, *J. Chem. Phys.* **1993**, 98, 5648-5652.
- [11] C. Lee, W. Yang and R.G. Parr, *Phys. Rev.* **1988**, B37, 785.
- [12] B. Miehlich, A. Savin, H. Stoll and H. Preuss , *Chem. Phys. Lett.*, **1988**, 157, 200-206.
- [14] G.N. Lewis; *J. Am. Chem. Soc.*, **1924**, 46 (9)2027-32.
- [15] T. oda, Pasquarellon Alfredo *Physical Rev.*, **2004**, B 70,134402.
- [16] L. Hernandez, *J. Chem. Physics*, **2000**,113(10), 4139-45.
- I. Roeggen, *Chem. Phys. Letters* , **1989**, 157(5), 409-14.
- [17] Fleming, *Frontier Orbitals and Organic Chemical Reactions*, John Wiley and Sons, New York, **1976**.